

Working Comprehensive List of research in combinatorics education

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CONFERENCE PROCEEDINGS

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North American Chapter of the International Group for the Psychology of Mathematics Education, Atlanta, GA: Georgia State University.

(Halani, Tillema, Kavousian, Engelke, Cadwallader Osker, etc.)

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DISSERTATIONS

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